

# Package ‘DelayedTensor’

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**Title** R package for sparse and out-of-core arithmetic and decomposition of Tensor

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**Description** DelayedTensor operates Tensor arithmetic directly on DelayedArray object. DelayedTensor provides some generic function related to Tensor arithmetic/decomposition and dispatches it on the DelayedArray class. DelayedTensor also supports Tensor contraction by einsum function, which is inspired by numpy einsum.

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DelayedTensor-package *R package for sparse and out-of-core arithmetic and decomposition of Tensor*

---

## Description

DelayedTensor operates Tensor arithmetic directly on DelayedArray object. DelayedTensor provides some generic function related to Tensor arithmetic/decomposition and dispatches it on the DelayedArray class. DelayedTensor also supports Tensor contraction by einsum function, which is inspired by numpy einsum.

## Details

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## Author(s)

Koki Tsuyuzaki [aut, cre]

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## See Also

# Unfold operations [unfold](#), [k\\_unfold](#), [matvec](#), [rs\\_unfold](#), [cs\\_unfold](#), [ttl](#) # Fold operations [fold](#), [k\\_fold](#), [unmatvec](#), [rs\\_fold](#), [cs\\_fold](#), [ttm](#) # Vectorization [vec](#) # Norm operations [fnorm](#), [innerProd](#) # Diagonal operations / Diagonal Tensor [diag](#), [DelayedDiagonalArray](#) # Mode-wise operations [modeSum](#), [modeMean](#) # Tensor product operations [hadamard](#), [hadamard\\_list](#), [kronecker](#), [kronecker\\_list](#), [khatri-rao](#), [khatri-rao\\_list](#) # Utilities [list\\_rep](#), [modebind\\_list](#), [rbind\\_list](#), [cbind\\_list](#) # Decomposition operations [hosvd](#), [cp](#), [tucker](#), [mpca](#), [pvd](#) # Einsum operation [einsum](#)

## Examples

```
ls("package:DelayedTensor")
```

---

<code>cbind_list</code>	<i>Mode-binding against list</i>
-------------------------	----------------------------------

---

## Description

Returns the binded DelayedArray in column space.

## Usage

```
cbind_list(L)
```

**Arguments**

L                      list of 2D DelayedArray

**Details**

This is a wrapper function to [modebind\\_list](#), when the DelayedArrays are 2D.

**Value**

2D DelayedArray object

**Note**

The dimensions of column in each DelayedArray must match.

**See Also**

[modebind\\_list](#)

**Examples**

```
library("DelayedRandomArray")
dlizt <- list(
  'darr1' = RandomUnifArray(c(2,3)),
  'darr2' = RandomUnifArray(c(2,3)))
cbind_list(dlizt)
```

---

cp-methods

*Canonical Polyadic Decomposition*

---

**Description**

Canonical Polyadic (CP) decomposition of a tensor, aka CANDECOMP/PARAFRAC. Approximate a K-Tensor using a sum of num\_components rank-1 K-Tensors. A rank-1 K-Tensor can be written as an outer product of K vectors. There are a total of num\_components \* darr@num\_modes vectors in the output, stored in darr@num\_modes matrices, each with num\_components columns. This is an iterative algorithm, with two possible stopping conditions: either relative error in Frobenius norm has gotten below tol, or the max\_iter number of iterations has been reached. For more details on CP decomposition, consult Kolda and Bader (2009).

**Usage**

```
cp(darr, num_components=NULL, max_iter=25, tol=1e-05)

## S4 method for signature 'DelayedArray'
cp(darr, num_components, max_iter, tol)
```

**Arguments**

darr	Tensor with K modes
num_components	the number of rank-1 K-Tensors to use in approximation
max_iter	maximum number of iterations if error stays above tol
tol	relative Frobenius norm error tolerance

**Details**

This function is an extension of the [cp](#) by DelayedArray.

Uses the Alternating Least Squares (ALS) estimation procedure. A progress bar is included to help monitor operations on large tensors.

**Value**

a list containing the following

lambdas	a vector of normalizing constants, one for each component
U	a list of matrices - one for each mode - each matrix with num_components columns
conv	whether or not $\text{resid} < \text{tol}$ by the last iteration
norm_percent	the percent of Frobenius norm explained by the approximation
est	estimate of darr after compression
fnorm_resid	the Frobenius norm of the error $\text{fnorm}(\text{est} - \text{darr})$
all_resids	vector containing the Frobenius norm of error for all the iterations

**References**

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

**See Also**

[tucker](#)

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(3,4,5))
cp(darr, num_components=2)
```

**Description**

The inverse operation to [cs\\_unfold](#).

**Usage**

```
cs_fold(mat, m = NULL, modes = NULL)

## S4 method for signature 'DelayedArray'
cs_fold(mat, m, modes)
```

**Arguments**

mat	DelayedArray object (only 2D)
m	the mode corresponding to cs_unfold
modes	the original modes of the DelayedArray

**Details**

This function is an extension of the [cs\\_fold](#) by DelayedArray.  
This is a wrapper function to [fold](#).

**Value**

DelayedArray (higher than 2D)

**References**

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

**See Also**

[fold](#), [cs\\_unfold](#)

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
matT3 <- DelayedTensor::cs_unfold(darr, m=3)
identical(
  as.array(DelayedTensor::cs_fold(matT3, m=3, modes=c(2,3,4))),
  as.array(darr))
```

## Description

Please see [matvec](#) and [unfold](#).

## Usage

```
cs_unfold(darr, m)

## S4 method for signature 'DelayedArray'
cs_unfold(darr, m)
```

## Arguments

darr	DelayedArray object
m	mode to be unfolded on

## Details

This function is an extension of the [cs\\_unfold](#) by DelayedArray.

This is a wrapper function to [unfold](#).

## Value

DelayedArray (2D)

## See Also

[unfold](#), [cs\\_fold](#)

## Examples

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
DelayedTensor::cs_unfold(darr, m=3)
```

DelayedDiagonalArray    *Diagonal DelayedArray*

---

## Description

Constructor of the diagonal of a DelayedArray.

## Usage

```
DelayedDiagonalArray(shape, value)
```

## Arguments

shape	Shape of DelayedArray (mode of Tensor)
value	either a single value or a vector. This argument is optional. If nothing is specified, 1s are filled with each diagonal element.

## Details

See also [diag](#) or [diag](#).

## Value

DelayedArray object

## References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

## See Also

[diag](#), [diag](#)

## Examples

```
darr <- DelayedDiagonalArray(2:4, 5)
DelayedTensor::diag(darr)
```



**Description**

Extract or replace the diagonal of a DelayedArray, or substitute the elements to the diagonal DelayedArray.

**Usage**

```
diag(darr)
diag(darr) <- value

## S4 method for signature 'DelayedArray'
diag(darr)
## S4 replacement method for signature 'DelayedArray'
diag(darr) <- value
```

**Arguments**

darr	DelayedArray object
value	either a single value or a vector of length equal to that of the current diagonal. Should be of a mode which can be coerced to that of darr.

**Details**

See also [DelayedDiagonalArray](#) or [diag](#).

**Value**

1D DelayedArray (vector) with length `min(dim(darr))`

**References**

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

**See Also**

[DelayedDiagonalArray](#)

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
DelayedTensor::diag(darr)
DelayedTensor::diag(darr)[1] <- 11111
DelayedTensor::diag(darr)[2] <- 22222
DelayedTensor::diag(darr)
```

---

 einsum

*Einstein Summation of DelayedArray*


---

## Description

Einstein summation is a convenient and concise notation for operations on n-dimensional arrays.

NOTE: Sparse mode of einsum is not available for now.

## Usage

```
einsum(subscripts, ...)
```

## Arguments

subscripts	a string in Einstein notation where arrays are separated by ',' and the result is separated by '->'. For example "ij,jk->ik" corresponds to a standard matrix multiplication. Whitespace inside the subscripts is ignored. Unlike the equivalent functions in Python, einsum only supports the explicit mode. This means that the subscripts must contain '->'. ...
...	the DelayedArrays that are combined.

## Details

This function is an extension of the [einsum](#) by DelayedArray.

## Value

The einsum function returns an array with one dimension for each index in the result of the subscripts. For example "ij,jk->ik" produces a 2-dimensional array, "abc,cd,de->abe" produces a 3-dimensional array.

## Examples

```
library("DelayedArray")
library("DelayedRandomArray")
darr1 <- RandomUnifArray(c(4,8))
darr2 <- RandomUnifArray(c(8,3))

# Matrix Multiply
darr1 %*% darr2
DelayedTensor::einsum("ij,jk -> ik", darr1, darr2)

# Diag
mat_sq <- RandomUnifArray(c(4,4))
DelayedTensor::diag(mat_sq)
einsum("ii->i", mat_sq)

# Trace
```

```

sum(DelayedTensor::diag(mat_sq))
einsum("ii->", mat_sq)

# Scalar product
darr3 <- RandomUnifArray(c(4,8))
darr3 * darr1
einsum("ij,ij->ij", darr3, darr1)

# Transpose
t(darr1)
einsum("ij->ji", darr1)

# Batched L2 norm
arr1 <- as.array(darr1)
arr3 <- as.array(darr3)
darr4 <- DelayedArray(array(c(arr1, arr3), dim = c(dim(arr1), 2)))

c(sum(darr1^2), sum(darr3^2))
einsum("ijb,ijb->b", darr4, darr4)

```

fnorm-methods

*Tensor Frobenius Norm of DelayedArray***Description**

Returns the Frobenius norm of the Tensor instance.

**Usage**

```

fnorm(darr)

## S4 method for signature 'DelayedArray'
fnorm(darr)

```

**Arguments**

darr                  DelayedArray object

**Details**

This function is an extension of the [fnorm](#) by DelayedArray.

**Value**

numeric Frobenius norm of darr

**Examples**

```

library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
fnorm(darr)

```

## Description

General folding of a 2D DelayedArray into a higher-order DelayedArray(Tensor). This is designed to be the inverse function to [unfold](#), with the same ordering of the indices. This amounts to following: if we were to unfold a Tensor using a set of `row_idx` and `col_idx`, then we can fold the resulting matrix back into the original Tensor using the same `row_idx` and `col_idx`.

## Usage

```
fold(mat, row_idx = NULL, col_idx = NULL, modes = NULL)
```

```
## S4 method for signature 'DelayedArray'
fold(mat, row_idx, col_idx, modes)
```

## Arguments

<code>mat</code>	DelayedArray object (only 2D)
<code>row_idx</code>	the indices of the modes that are mapped onto the row space
<code>col_idx</code>	the indices of the modes that are mapped onto the column space
<code>modes</code>	the modes of the output DelayedArray

## Details

This function is an extension of the [fold](#) by DelayedArray.

## Value

DelayedArray object with modes given by `modes`

## References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

## See Also

[unfold](#), [k\\_fold](#), [unmatvec](#), [rs\\_fold](#), [cs\\_fold](#)

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
matT3 <- DelayedTensor::unfold(darr, row_idx=2, col_idx=c(3,1))
identical(
  as.array(DelayedTensor::fold(matT3, row_idx=2, col_idx=c(3,1),
    modes=c(2,3,4))),
  as.array(darr))
```

---

getSparse	<i>Getter of the intermediate/output DelayedArray object in DelayedTensor</i>
-----------	---

---

**Description**

Whether the intermediate and output DelayedArray used in DelayedTensor is used as sparse tensor or not.

NOTE: Sparse mode is experimental! Whether it contributes to higher speed and lower memory is quite dependent on the sparsity of the DelayedArray, and the current implementation does not recognize the block size, which may cause Out-of-Memory errors.

**Usage**

```
getSparse()
```

**Value**

TRUE or FALSE (Default: FALSE)

**Examples**

```
getSparse()
```

---

getVerbose	<i>Getter function to control the verbose messages from DelayedTensor</i>
------------	---

---

**Description**

Returns the verbose setting of DelayedTensor functions.

**Usage**

```
getVerbose()
```

**Value**

TRUE or FALSE (Default: FALSE)

**Examples**

```
getVerbose()
```

---

hadamard-methods

*Hadamard Product of DelayedArray*


---

**Description**

Returns the Hadamard product of two Tensors. Commonly used for n-mode products and various Tensor decompositions.

**Usage**

```
hadamard(darr1, darr2)
```

```
## S4 method for signature 'DelayedArray,DelayedArray'
hadamard(darr1, darr2)
```

**Arguments**

darr1	first DelayedArray object
darr2	second DelayedArray object

**Value**

matrix that is the Hadamard product

**Note**

The modes/dimensions of each element of two Tensors must match.

**See Also**

[khatri\\_rao](#), [khatri\\_rao\\_list](#), [kronecker](#), [kronecker\\_list](#), [hadamard\\_list](#)

**Examples**

```
library("DelayedRandomArray")
darr1 <- RandomUnifArray(c(2,4))
darr2 <- RandomUnifArray(c(2,4))
hadamard(darr1, darr1)
```

---

hadamard_list	<i>Hadamard Product against list</i>
---------------	--------------------------------------

---

## Description

Returns the hadamard (element-wise) product from a list of matrices or vectors. Commonly used for n-mode products and various Tensor decompositions.

## Usage

```
hadamard_list(L)
```

## Arguments

L                      list of DelayedArray

## Details

This function is an extension of the [hadamard\\_list](#) by DelayedArray.

## Value

matrix that is the Hadamard product

## Note

The modes/dimensions of each element in the list must match.

## See Also

[khatri\\_rao](#), [khatri\\_rao\\_list](#), [kronecker](#), [kronecker\\_list](#), [hadamard](#)

## Examples

```
library("DelayedRandomArray")
dlizt <- list(
  'darr1' = RandomUnifArray(c(2,3,4)),
  'darr2' = RandomUnifArray(c(2,3,4)))
hadamard_list(dlizt)
```

---

 hosvd-methods

 (Truncated-)Higher-order SVD
 

---

## Description

Higher-order SVD of a K-Tensor. Write the K-Tensor as a (m-mode) product of a core Tensor (possibly smaller modes) and K orthogonal factor matrices. Truncations can be specified via ranks (making them smaller than the original modes of the K-Tensor will result in a truncation). For the mathematical details on HOSVD, consult Lathauwer et. al. (2000).

## Usage

```
hosvd(darr, ranks=NULL)

## S4 method for signature 'DelayedArray'
hosvd(darr, ranks)
```

## Arguments

darr	Tensor with K modes
ranks	a vector of desired modes in the output core tensor, default is darr@modes

## Details

This function is an extension of the [hosvd](#) by DelayedArray.

A progress bar is included to help monitor operations on large tensors.

## Value

a list containing the following:

Z core tensor with modes specified by ranks

U a list of orthogonal matrices, one for each mode

est estimate of darr after compression

fnorm\_resid the Frobenius norm of the error  $\text{fnorm}(\text{est}-\text{darr})$  - if there was no truncation, then this is on the order of  $\text{mach\_eps} * \text{fnorm}$ .

## Note

The length of ranks must match darr@num\_modes.

## References

L. Lathauwer, B.Moor, J. Vanderwalle "A multilinear singular value decomposition". Journal of Matrix Analysis and Applications 2000.



**See Also**[tucker](#)**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(3,4,5))
hosvd(darr, ranks=c(2,1,3))
```

---

human_mid_brain	<i>Matrix object of human mid brain data</i>
-----------------	--

---

**Description**

A matrix with 500 rows (genes) \* 1977 columns (cells).

**Usage**

```
data(human_mid_brain)
```

**Details**

The data matrix is downloaded from GEO Series GSE76381 (<https://www.ncbi.nlm.nih.gov/geo/download/?acc=GSE76381&>)  
For the details, see inst/script/make-data.R.

**References**

Y-h. Taguchi and T. Turki (2019) Tensor Decomposition-Based Unsupervised Feature Extraction Applied to Single-Cell Gene Expression Analysis. *Frontiers in Genetics*, **10(864)**: 10:3389/fgene.2019.00864

**See Also**[mouse\\_mid\\_brain](#)**Examples**

```
data(human_mid_brain)
```

---

innerProd-methods	<i>Tensors Inner Product of DelayedArray</i>
-------------------	--

---

**Description**

Returns the inner product between two Tensors

**Usage**

```
innerProd(darr1, darr2)

## S4 method for signature 'DelayedArray,DelayedArray'
innerProd(darr1, darr2)
```

**Arguments**

darr1	first DelayedArray object
darr2	second DelayedArray object

**Details**

This function is an extension of the [innerProd](#) by DelayedArray.

**Value**

inner product between darr1 and darr2

**Examples**

```
library("DelayedRandomArray")
darr1 <- RandomUnifArray(c(2,3,4))
darr2 <- RandomUnifArray(c(2,3,4))
innerProd(darr1, darr2)
```

---

khatri_rao-methods	<i>Khatri-Rao Product of DelayedArray</i>
--------------------	---

---

**Description**

Returns the Khatri-Rao (column-wise Kronecker) product of two matrices. If the inputs are vectors then this is the same as the Kronecker product.

**Usage**

```
khatri_rao(darr1, darr2)

## S4 method for signature 'DelayedArray,DelayedArray'
khatri_rao(darr1, darr2)
```

**Arguments**

darr1	first DelayedArray object
darr2	second DelayedArray object

**Details**

This function is an extension of the [khatri\\_rao](#) by DelayedArray.

**Value**

matrix that is the Khatri-Rao product

**Note**

The number of columns must match in the two inputs.

**See Also**

[hadamard](#), [hadamard\\_list](#), [kronecker](#), [kronecker\\_list](#), [khatri\\_rao\\_list](#)

**Examples**

```
library("DelayedRandomArray")
darr1 <- RandomUnifArray(c(2,4))
darr2 <- RandomUnifArray(c(3,4))
khatri_rao(darr1, darr2)
```

---

khatri_rao_list	<i>Khatri-Rao Product against list</i>
-----------------	--

---

**Description**

Returns the Khatri-Rao product from a list of matrices or vectors. Commonly used for n-mode products and various Tensor decompositions.

**Usage**

```
khatri_rao_list(L, reverse = FALSE)
```

**Arguments**

L	list of DelayedArray
reverse	whether or not to reverse the order

**Details**

This function is an extension of the [khatri\\_rao\\_list](#) by DelayedArray.

**Value**

matrix that is the Khatri-Rao product

**Note**

The number of columns must match in every element of the input list.

**See Also**

[hadamard](#), [hadamard\\_list](#), [kronecker](#), [kronecker\\_list](#), [khatri\\_rao](#)

**Examples**

```
library("DelayedRandomArray")
darr1 <- RandomUnifArray(c(2,3))
dlizt <- list(
  'darr1' = RandomUnifArray(c(2,4)),
  'darr2' = RandomUnifArray(c(3,4)))
khatri_rao_list(dlizt)
```

---

kronecker-methods

*Kronecker Product of DelayedArray*


---

**Description**

Returns the Kronecker product of two Tensors. Commonly used for n-mode products and various Tensor decompositions.

**Usage**

```
kronecker(darr1, darr2)

## S4 method for signature 'DelayedArray,DelayedArray'
kronecker(darr1, darr2)
```

**Arguments**

darr1	first DelayedArray object
darr2	second DelayedArray object

**Value**

matrix that is the Kronecker product

**See Also**

[khatri\\_rao](#), [khatri\\_rao\\_list](#), [hadamard](#), [hadamard\\_list](#), [kronecker\\_list](#)

**Examples**

```
library("DelayedRandomArray")
darr1 <- RandomUnifArray(c(2,3))
darr2 <- RandomUnifArray(c(4,5))
kronecker(darr1, darr2)
```

---

kronecker_list	<i>Kronecker Product against list</i>
----------------	---------------------------------------

---

**Description**

Returns the Kronecker product from a list of matrices or vectors. Commonly used for n-mode products and various Tensor decompositions.

**Usage**

```
kronecker_list(L)
```

**Arguments**

L                      list of DelayedArray

**Details**

This function is an extension of the [kronecker\\_list](#) by DelayedArray.

**Value**

matrix that is the Kronecker product

**See Also**

[khatri\\_rao](#), [khatri\\_rao\\_list](#), [hadamard](#), [hadamard\\_list](#), [kronecker](#)

**Examples**

```
library("DelayedRandomArray")
dlizt <- list(
  'darr1' = RandomUnifArray(c(2,3,4)),
  'darr2' = RandomUnifArray(c(2,3,4))
)
kronecker_list(dlizt)
```

---

k_fold-methods	<i>k-mode Folding of 2D DelayedArray</i>
----------------	--

---

**Description**

k-mode folding of a matrix into a Tensor. This is the inverse function to `k_unfold` in the `m` mode. In particular, `k_fold(k_unfold(darr, m), m, dim(darr))` will result in the original Tensor.

**Usage**

```
k_fold(mat, m = NULL, modes = NULL)

## S4 method for signature 'DelayedArray'
k_fold(mat, m, modes)
```

**Arguments**

<code>mat</code>	DelayedArray object (only 2D)
<code>m</code>	the index of the mode that is mapped onto the row indices
<code>modes</code>	the modes of the output DelayedArray

**Details**

This function is an extension of the `k_fold` by DelayedArray.  
This is a wrapper function to `fold`.

**Value**

DelayedArray object with modes given by `modes`

**References**

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

**See Also**

`fold`, `k_unfold`

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
matT2 <- k_unfold(darr, m=2)
identical(
  as.array(k_fold(matT2, m=2, modes=c(2,3,4))),
  as.array(darr))
```

---

k_unfold-methods	<i>Tensor k-mode Unfolding of DelayedArray</i>
------------------	--

---

## Description

Unfolding of a tensor by mapping the  $k$ th mode (specified through parameter  $m$ ), and all other modes onto the column space. This is the most common type of unfolding operation for Tucker decompositions and its variants. Also known as  $k$ -mode matricization.

## Usage

```
k_unfold(darr, m)

## S4 method for signature 'DelayedArray'
k_unfold(darr, m)
```

## Arguments

darr	DelayedArray object
m	the index of the mode to unfold on

## Details

This function is an extension of the [k\\_unfold](#) by DelayedArray.

This is a wrapper function to [unfold](#).

See also `k_unfold(darr, m=NULL)`

## Value

matrix with `dim(darr)[m]` rows and `prod(dim(darr)[-m])` columns

## References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

## See Also

[unfold](#), [k\\_fold](#)

## Examples

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
rs_unfold(darr, m=2)
```

---

list_rep	<i>Replicate of arbitrary object</i>
----------	--------------------------------------

---

**Description**

Returns the replicates of base object x.

**Usage**

```
list_rep(x, n=NULL)
```

**Arguments**

x	Any object
n	Number of replicate

**Value**

List

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
list_rep(darr, 3)
```

---

matvec-methods	<i>Tensor Matvec Unfolding of DelayedArray</i>
----------------	--

---

**Description**

For 3-tensors only. Stacks the slices along the third mode.

**Usage**

```
matvec(darr)

## S4 method for signature 'DelayedArray'
matvec(darr)
```

**Arguments**

darr	DelayedArray object
------	---------------------



**Details**

This function is an extension of the [matvec](#) by DelayedArray.

This is a wrapper function to [unfold](#).

**Value**

matrix with `prod(dim(darr)[-m])` rows and `dim(darr)[m]` columns

**References**

M. Kilmer, K. Braman, N. Hao, and R. Hoover, "Third-order tensors as operators on matrices: a theoretical and computational framework with applications in imaging". SIAM Journal on Matrix Analysis and Applications 2013.

**See Also**

[unfold](#), [unmatvec](#)

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
matvec(darr)
```

---

modebind_list	<i>Mode-binding against list</i>
---------------	----------------------------------

---

**Description**

Returns the binded DelayedArray in mode-m.

**Usage**

```
modebind_list(L, m=NULL)
```

**Arguments**

L	list of DelayedArray
m	list of DelayedArray

**Value**

DelayedArray object

**Note**

The dimensions of mode m must match.

**See Also**

[rbind\\_list](#), [cbind\\_list](#)

**Examples**

```
library("DelayedRandomArray")
dlizt <- list(
  'darr1' = RandomUnifArray(c(2,3,4)),
  'darr2' = RandomUnifArray(c(2,3,4)))
modebind_list(dlizt, m=1)
modebind_list(dlizt, m=2)
modebind_list(dlizt, m=3)
```

---

modeMean-methods

*Tensor Mean Across Single Mode of DelayedArray*


---

**Description**

Given a mode for a K-tensor, this returns the K-1 tensor resulting from taking the mean across that particular mode.

**Usage**

```
modeMean(darr, m = NULL, drop = FALSE)

## S4 method for signature 'DelayedArray'
modeMean(darr, m, drop)
```

**Arguments**

darr	DelayedArray object
m	the index of the mode to average across
drop	whether or not mode m should be dropped

**Details**

This function is an extension of the [modeMean](#) by DelayedArray.

NOTE: Sparse mode of modeMean is not available for now.

```
modeMean(darr, m=NULL, drop=FALSE)
```

**Value**

K-1 or K Tensor, where  $K = \text{length}(\text{dim}(\text{darr}))$

**See Also**

[modeSum](#)

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(1,2,3))
modeMean(darr, 1, drop=FALSE)
modeMean(darr, 1, drop=TRUE)
modeMean(darr, 2)
modeMean(darr, 3)
```

modeSum-methods

*Tensor Sum Across Single Mode of DelayedArray***Description**

Given a mode for a K-tensor, this returns the K-1 tensor resulting from summing across that particular mode.

**Usage**

```
modeSum(darr, m = NULL, drop = FALSE)

## S4 method for signature 'DelayedArray'
modeSum(darr, m, drop)
```

**Arguments**

darr	DelayedArray object
m	the index of the mode to sum across
drop	whether or not mode m should be dropped

**Details**

This function is an extension of the [modeSum](#) by DelayedArray.

NOTE: Sparse mode of modeSum is not available for now.

```
modeSum(darr, m=NULL, drop=FALSE)
```

**Value**

K-1 or K tensor, where  $K = \text{length}(\text{dim}(\text{darr}))$

**See Also**

[modeMean](#)

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(1,2,3))
modeSum(darr, 1, drop=FALSE)
modeSum(darr, 1, drop=TRUE)
modeSum(darr, 2)
modeSum(darr, 3)
```

---

mouse_mid_brain	<i>Matrix object of mouse mid brain data</i>
-----------------	--

---

**Description**

A matrix with 500 rows (genes) \* 1907 columns (cells).

**Usage**

```
data(mouse_mid_brain)
```

**Details**

The data matrix is downloaded from GEO Series GSE76381 (<https://www.ncbi.nlm.nih.gov/geo/download/?acc=GSE76381&>)  
For the details, see `inst/script/make-data.R`.

**References**

Y-h. Taguchi and T. Turki (2019) Tensor Decomposition-Based Unsupervised Feature Extraction Applied to Single-Cell Gene Expression Analysis. *Frontiers in Genetics*, **10(864)**: 10:3389/fgene.2019.00864

**See Also**

[mouse\\_mid\\_brain](#)

**Examples**

```
data(mouse_mid_brain)
```

## Description

This is basically the Tucker decomposition of a K-Tensor, [tucker](#), with one of the modes uncompressed. If  $K = 3$ , then this is also known as the Generalized Low Rank Approximation of Matrices (GLRAM). This implementation assumes that the last mode is the measurement mode and hence uncompressed. This is an iterative algorithm, with two possible stopping conditions: either relative error in Frobenius norm has gotten below `tol`, or the `max_iter` number of iterations has been reached. For more details on the MPCA of tensors, consult Lu et al. (2008).

## Usage

```
mpca(darr, ranks=NULL, max_iter=25, tol=1e-05)

## S4 method for signature 'DelayedArray'
mpca(darr, ranks, max_iter, tol)
```

## Arguments

<code>darr</code>	Tensor with K modes
<code>ranks</code>	a vector of the compressed modes of the output core Tensor, this has length K-1
<code>max_iter</code>	maximum number of iterations if error stays above <code>tol</code>
<code>tol</code>	relative Frobenius norm error tolerance

## Details

This function is an extension of the [mpca](#) by DelayedArray.

Uses the Alternating Least Squares (ALS) estimation procedure. A progress bar is included to help monitor operations on large tensors.

## Value

a list containing the following:

- `Z_ext` the extended core tensor, with the first K-1 modes given by `ranks`
- `U` a list of K-1 orthogonal factor matrices - one for each compressed mode, with the number of columns of the matrices given by `ranks`
- `conv` whether or not  $\text{resid} < \text{tol}$  by the last iteration
- `est` estimate of `darr` after compression
- `norm_percent` the percent of Frobenius norm explained by the approximation
- `fnorm_resid` the Frobenius norm of the error `fnorm(est-darr)`
- `all_resids` vector containing the Frobenius norm of error for all the iterations

**Note**

The length of ranks must match `darr@num_modes-1`.

**References**

H. Lu, K. Plataniotis, A. Venetsanopoulos, "Mpca: Multilinear principal component analysis of tensor objects". IEEE Trans. Neural networks, 2008.

**See Also**

[tucker](#), [hosvd](#)

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(3,4,5))
mpca(darr, ranks=c(1,2))
```

---

outerProd-methods

*Tensors Outer Product of DelayedArray*

---

**Description**

Returns the outer product between two Tensors

**Usage**

```
outerProd(darr1, darr2)

## S4 method for signature 'DelayedArray,DelayedArray'
outerProd(darr1, darr2)
```

**Arguments**

<code>darr1</code>	first DelayedArray object
<code>darr2</code>	second DelayedArray object

**Details**

NOTE: Sparse mode of `outerProd` is not available for now.

**Value**

outer product between `darr1` and `darr2`

## Examples

```
library("DelayedRandomArray")
darr1 <- RandomUnifArray(c(2,3))
darr2 <- RandomUnifArray(c(4,5))
outerProd(darr1, darr2)
```

---

pvd-methods

*Population Value Decomposition*


---

## Description

The default Population Value Decomposition (PVD) of a series of 2D images. Constructs population-level matrices  $P$ ,  $V$ , and  $D$  to account for variances within as well as across the images. Structurally similar to Tucker ([tucker](#)) and GLRAM ([mpca](#)), but retains crucial differences. Requires  $2 \times n_3 + 2$  parameters to specified the final ranks of  $P$ ,  $V$ , and  $D$ , where  $n_3$  is the third mode (how many images are in the set). Consult Crainiceanu et al. (2013) for the construction and rationale behind the PVD model.

## Usage

```
pvd(darr, uranks=NULL, wranks=NULL, a=NULL, b=NULL)
```

```
## S4 method for signature 'DelayedArray'
pvd(darr, uranks, wranks, a, b)
```

## Arguments

darr	3D DelayedArray (Tensor) with the third mode being the measurement mode
uranks	ranks of the $U$ matrices
wranks	ranks of the $W$ matrices
a	rank of $P = U\%*\%t(U)$
b	rank of $D = W\%*\%t(W)$

## Details

This function is an extension of the [pvd](#) by DelayedArray.

The PVD is not an iterative method, but instead relies on  $n_3 + 2$  separate PCA decompositions. The third mode is for how many images are in the set.

## Value

a list containing the following:

$P$  population-level matrix  $P = U\%*\%t(U)$ , where  $U$  is constructed by stacking the truncated left eigenvectors of slice-wise PCA along the third mode

$V$  a list of image-level core matrices

D population-level matrix  $D = W W^T$ , where W is constructed by stacking the truncated right eigenvectors of slice-wise PCA along the third mode

est estimate of darr after compression

norm\_percent the percent of Frobenius norm explained by the approximation

fnorm\_resid the Frobenius norm of the error  $f_{\text{norm}}(\text{est} - \text{darr})$

**References**

C. Crainiceanu, B. Caffo, S. Luo, V. Zipunnikov, N. Punjabi, "Population value decomposition: a framework for the analysis of image populations". Journal of the American Statistical Association, 2013.

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(3,4,5))
pvd(darr, uranks=rep(2,5), wranks=rep(3,5), a=2, b=3)
```

---

rbind_list	<i>Mode-binding against list</i>
------------	----------------------------------

---

**Description**

Returns the binded DelayedArray in row space.

**Usage**

```
rbind_list(L)
```

**Arguments**

L                      list of 2D DelayedArray

**Details**

This is a wrapper function to [modebind\\_list](#), when the DelayedArrays are 2D.

**Value**

2D DelayedArray object

**Note**

The dimensions of row in each DelayedArray must match.

**See Also**

[modebind\\_list](#)



**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
dlizt <- list(
  'darr1' = RandomUnifArray(c(2,3)),
  'darr2' = RandomUnifArray(c(2,3)))
rbind_list(dlizt)
```

rs\_fold-methods

*Row Space Folding of 2D DelayedArray***Description**

The inverse operation to [rs\\_unfold](#).

**Usage**

```
rs_fold(mat, m = NULL, modes = NULL)

## S4 method for signature 'DelayedArray'
rs_fold(mat, m, modes)
```

**Arguments**

mat	DelayedArray object (only 2D)
m	the mode corresponding to <a href="#">rs_unfold</a>
modes	the original modes of the DelayedArray

**Details**

This function is an extension of the [rs\\_fold](#) by DelayedArray.

This is a wrapper function to [fold](#).

**Value**

DelayedArray (higher than 2D)

**References**

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

**See Also**

[fold](#), [rs\\_unfold](#)

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
matT2 <- rs_unfold(darr, m=2)
identical(
  as.array(rs_fold(matT2, m=2, modes=c(2,3,4))),
  as.array(darr))
```

---

rs_unfold-methods	<i>Tensor Row Space Unfolding of DelayedArray</i>
-------------------	---

---

**Description**

Please see [k\\_unfold](#) and [unfold](#).

**Usage**

```
rs_unfold(darr, m)

## S4 method for signature 'DelayedArray'
rs_unfold(darr, m)
```

**Arguments**

darr	DelayedArray object
m	mode to be unfolded on

**Details**

This function is an extension of the [rs\\_unfold](#) by DelayedArray.

This is a wrapper function to [unfold](#).

See also `rs_unfold(darr, m=NULL)`

**Value**

DelayedArray (2D)

**See Also**

[unfold](#), [rs\\_fold](#)

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
matT2 <- rs_unfold(darr, m=2)
```

---

setSparse	<i>Setter to set the intermediate DelayedArray object in DelayedTensor</i>
-----------	--

---

**Description**

Set whether the intermediate and output DelayedArray used in DelayedTensor is used as sparse tensor or not.

NOTE: Sparse mode is experimental! Whether it contributes to higher speed and lower memory is quite dependent on the sparsity of the DelayedArray, and the current implementation does not recognize the block size, which may cause Out-of-Memory errors.

**Usage**

```
setSparse(as.sparse=FALSE)
```

**Arguments**

as.sparse      TRUE or FALSE (Default: FALSE)

**Value**

Nothing

**Examples**

```
setSparse(TRUE)
setSparse(FALSE)
```

---

setVerbose	<i>Setter to set the verbose mode of DelayedTensor</i>
------------	--

---

**Description**

Set the verbose message to monitor the block-processing procedure.

**Usage**

```
setVerbose(as.verbose=FALSE)
```

**Arguments**

as.verbose      TRUE or FALSE (Default: FALSE)

**Value**

Nothing

**Examples**

```
setVerbose(TRUE)
setVerbose(FALSE)
```

---

ttl	<i>DelayedArray Times List</i>
-----	--------------------------------

---

**Description**

Contracted (m-Mode) product between a Tensor of arbitrary number of modes and a list of matrices. The result is folded back into Tensor.

**Usage**

```
ttl(darr, list_mat, ms=NULL)
```

**Arguments**

darr	DelayedArray object with K modes
list_mat	a list of 2D DelayedArray objects
ms	a vector of modes to contract on (order should match the order of list_mat)

**Details**

This function is an extension of the [ttl](#) by DelayedArray.

This is a wrapper function to [unfold](#).

Performs ttm repeated for a single Tensor and a list of matrices on multiple modes. For instance, suppose we want to do multiply a Tensor object darr with three matrices mat1, mat2, mat3 on modes 1, 2, and 3. We could do ttm(ttm(ttm(darr,mat1,1),mat2,2),3), or we could do ttl(darr,list(mat1,mat2,mat3),c(1,2,3)). The order of the matrices in the list should obviously match the order of the modes. This is a common operation for various Tensor decompositions such as CP and Tucker. For the math on the m-Mode Product, see Kolda and Bader (2009).

**Value**

DelayedArray object with K modes (Tensor)

**Note**

The returned Tensor does not drop any modes equal to 1.

**References**

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

**See Also**[ttm](#)**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(3,4,5))
dlizt <- list(
  'darr1' = RandomUnifArray(c(10,3)),
  'darr2' = RandomUnifArray(c(10,4)))
ttl(darr, dlizt, ms=c(1,2))
```

ttm-methods

*Tensor Times Matrix (m-Mode Product)***Description**

Contracted (m-Mode) product between a DelayedArray (Tensor) of arbitrary number of modes and a matrix. The result is folded back into Tensor.

**Usage**

```
ttm(darr, mat, m = NULL)

## S4 method for signature 'DelayedArray,DelayedArray'
ttm(darr, mat, m)
```

**Arguments**

darr	DelayedArray object
mat	input 2D DelayedArray with same number columns as the mth mode of darr
m	the mode to contract on

**Details**

This function is an extension of the [ttm](#) by DelayedArray.

By definition,  $\text{rs\_unfold}(\text{ttm}(\text{darr}, \text{mat}), m) = \text{mat} \% \% \text{rs\_unfold}(\text{darr}, m)$ , so the number of columns in mat must match the mth mode of darr. For the math on the m-Mode Product, see Kolda and Bader (2009).

**Value**

a DelayedArray object with K modes

**Note**

The mth mode of darr must match the number of columns in mat. By default, the returned Tensor does not drop any modes equal to 1.

## References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

## See Also

[rs\\_unfold](#), [ttl](#)

## Examples

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
mat <- RandomUnifArray(c(10,4))
ttm(darr, mat, m=3)
```

---

tucker-methods

*Tucker Decomposition*


---

## Description

The Tucker decomposition of a tensor. Approximates a K-Tensor using a n-mode product of a core tensor (with modes specified by ranks) with orthogonal factor matrices. If there is no truncation in one of the modes, then this is the same as the MPCA, [mpca](#). If there is no truncation in all the modes (i.e. ranks = darr@modes), then this is the same as the HOSVD, [hosvd](#). This is an iterative algorithm, with two possible stopping conditions: either relative error in Frobenius norm has gotten below tol, or the max\_iter number of iterations has been reached. For more details on the Tucker decomposition, consult Kolda and Bader (2009).

## Usage

```
tucker(darr, ranks=NULL, max_iter=25, tol=1e-05)

## S4 method for signature 'DelayedArray'
tucker(darr, ranks, max_iter, tol)
```

## Arguments

darr	Tensor with K modes
ranks	a vector of the modes of the output core Tensor
max_iter	maximum number of iterations if error stays above tol
tol	relative Frobenius norm error tolerance

## Details

This function is an extension of the [tucker](#) by DelayedArray.

Uses the Alternating Least Squares (ALS) estimation procedure also known as Higher-Order Orthogonal Iteration (HOOI). Initialized using a (Truncated-)HOSVD. A progress bar is included to help monitor operations on large tensors.

**Value**

a list containing the following:

- `Z` the core tensor, with modes specified by ranks
- `U` a list of orthogonal factor matrices - one for each mode, with the number of columns of the matrices given by ranks
- `conv` whether or not `resid < tol` by the last iteration
- `est` estimate of `darr` after compression
- `norm_percent` the percent of Frobenius norm explained by the approximation
- `fnorm_resid` the Frobenius norm of the error `fnorm(est-darr)`
- `all_resids` vector containing the Frobenius norm of error for all the iterations

**Note**

The length of ranks must match `darr@num_modes`.

**References**

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

**See Also**

[hosvd](#), [mpca](#)

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
tucker(darr, ranks=c(1,2,3))
```

---

unfold-methods

*Tensor Unfolding of 2D DelayedArray*

---

**Description**

Unfolds the tensor into a matrix, with the modes in `rs` onto the rows and modes in `cs` onto the columns. Note that `c(rs,cs)` must have the same elements (order doesn't matter) as `dim(darr)`. Within the rows and columns, the order of the unfolding is determined by the order of the modes. This convention is consistent with Kolda and Bader (2009).

**Usage**

```
unfold(darr, row_idx, col_idx)

## S4 method for signature 'DelayedArray'
unfold(darr, row_idx, col_idx)
```

**Arguments**

darr	DelayedArray object
row_idx	the indices of the modes to map onto the row space
col_idx	the indices of the modes to map onto the column space

**Details**

This function is an extension of the [unfold](#) by DelayedArray.

For Row Space Unfolding or m-mode Unfolding, see [rs\\_unfold](#). For Column Space Unfolding or matvec, see [cs\\_unfold](#).

[vec](#) returns the vectorization of the tensor.

**Value**

2D DelayedArray with `prod(row_idx)` rows and `prod(col_idx)` columns

**References**

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

**See Also**

[k\\_unfold](#), [matvec](#), [rs\\_unfold](#), [cs\\_unfold](#)

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
unfold(darr, row_idx=2, col_idx=c(3,1))
```

---

unmatvec-methods

*Unmatvec Folding of 2D DelayedArray*


---

**Description**

The inverse operation to [matvec-methods](#), turning a matrix into a Tensor. For a full account of matrix folding/unfolding operations, consult Kolda and Bader (2009).

**Usage**

```
unmatvec(mat, modes = NULL)

## S4 method for signature 'DelayedArray'
unmatvec(mat, modes)
```



**Arguments**

mat	DelayedArray object (only 2D)
modes	the modes of the output DelayedArray

**Details**

This function is an extension of the [unmatvec](#) by DelayedArray.

This is a wrapper function to [fold](#).

**Value**

DelayedArray object with modes given by modes

**References**

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

**See Also**

[fold](#), [matvec](#)

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
matT1 <- matvec(darr)
identical(
  as.array(unmatvec(matT1, modes=c(2,3,4))),
  as.array(darr))
```

**Description**

Change the dimension of DelayedArray from multi-dimension (e.g. array) to single-dimension (e.g. vector).

**Usage**

```
vec(darr)

## S4 method for signature 'DelayedArray'
vec(darr)
```

**Arguments**

darr                      DelayedArray object

**Details**

This function is an extension of the [vec](#) by DelayedArray.

**Value**

1D DelayedArray (vector) with length `prod(dim(darr))`

**References**

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

**Examples**

```
library("DelayedRandomArray")
darr <- RandomUnifArray(c(2,3,4))
vec(darr)
```

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