## Package 'diptest'

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Title Hartigan's Dip Test Statistic for Unimodality - Corrected

**Description** Compute Hartigan's dip test statistic for unimodality / multimodality and provide a test with simulation based p-values, where the original public code has been corrected.

Imports graphics, stats

BuildResaveData no

License GPL (>= 2)

URL https://github.com/mmaechler/diptest

BugReports https://github.com/mmaechler/diptest/issues

NeedsCompilation yes

**Repository** CRAN

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## **R** topics documented:

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dip

#### Description

Computes Hartigans' dip test statistic for testing unimodality, and additionally the modal interval.

#### Usage

```
dip(x, full.result = FALSE, min.is.0 = FALSE, debug = FALSE)
```

#### Arguments

x	numeric; the data.
full.result	logical or string; dip(., full.result=TRUE) returns the full result list; if "all" it additionally uses the mn and mj components to compute the initial GCM and LCM, see below.
min.is.0	logical indicating if the <b>min</b> imal value of the dip statistic $D_n$ can be zero or not. Arguably should be set to TRUE for internal consistency reasons, but is false by default both for continuity and backwards compatibility reasons, see the examples below.
debug	logical; if true, some tracing information is printed (from the C routine).

#### Value

depending on full.result either a number, the dip statistic, or an object of class "dip" which is a list with components

х	the sorted unname()d data.
n	length(x).
dip	the dip statistic
lo.hi	indices into x for lower and higher end of modal interval
xl, xu	lower and upper end of modal interval
gcm, lcm	(last used) indices for greatest convex minorant and the least concave majorant.
mn, mj	index vectors of length n for the GC minorant and the LC majorant respectively.

For "full" results of class "dip", there are print and plot methods, the latter with its own manual page.

dip

#### Note

For  $n \leq 3$  where  $n \leq length(x)$ , the dip statistic  $D_n$  is always the same minimum value, 1/(2n), i.e., there's no possible dip test. Note that up to May 2011, from Hartigan's original Fortran code, Dn was set to zero, when all x values were identical. However, this entailed discontinuous behavior, where for arbitrarily close data  $\tilde{x}$ ,  $D_n(\tilde{x}) = \frac{1}{2n}$ .

Yong Lu <lyongu+@cs.cmu.edu> found in Oct 2003 that the code was not giving symmetric results for mirrored data (and was giving results of almost 1, and then found the reason, a misplaced "")"' in the original Fortran code. This bug has been corrected for diptest version 0.25-0 (Feb 13, 2004).

Nick Cox (Durham Univ.) said (on March 20, 2008 on the Stata-list):

As it comes from a bimodal husband-wife collaboration, the name perhaps should be "*Hartigan-Hartigan dip test*", but that does not seem to have caught on. Some of my less statistical colleagues would sniff out the hegemony of patriarchy there, although which Hartigan is being overlooked is not clear.

Martin Maechler, as a Swiss, and politician, would say:

Let's find a compromise, and call it "*Hartigans' dip test*", so we only have to adapt orthography (:-).

#### Author(s)

Martin Maechler <maechler@stat.math.ethz.ch>, 1994, based on S (S-PLUS) and C code donated from Dario Ringach <dario@wotan.cns.nyu.edu> who had applied f2c on the original Fortran code available from Statlib.

In Aug.1993, recreated and improved Hartigans' "P-value" table, which later became qDiptab.

#### References

P. M. Hartigan (1985) Computation of the Dip Statistic to Test for Unimodality; *Applied Statistics* (*JRSS C*) **34**, 320–325.

Corresponding (buggy!) Fortran code of 'AS 217' available from Statlib, http://lib.stat.cmu. edu/apstat/217

J. A. Hartigan and P. M. Hartigan (1985) The Dip Test of Unimodality; Annals of Statistics 13, 70–84.

#### See Also

dip.test to compute the dip *and* perform the unimodality test, based on P-values, interpolated from qDiptab; isoreg for isotonic regression.

#### Examples

```
data(statfaculty)
plot(density(statfaculty))
rug(statfaculty, col="midnight blue"); abline(h=0, col="gray")
dip(statfaculty)
(dS <- dip(statfaculty, full = TRUE, debug = TRUE))
plot(dS)
## even more output -- + plot showing "global" GCM/LCM:
(dS2 <- dip(statfaculty, full = "all", debug = 3))</pre>
```

dip

dip.test

```
plot(dS2)
```

```
data(faithful)
fE <- faithful$eruptions</pre>
plot(density(fE))
rug(fE, col="midnight blue"); abline(h=0, col="gray")
dip(fE, debug = 2) ## showing internal work
(dE <- dip(fE, full = TRUE)) ## note the print method
plot(dE, do.points=FALSE)
data(precip)
plot(density(precip))
rug(precip, col="midnight blue"); abline(h=0, col="gray")
str(dip(precip, full = TRUE, debug = TRUE))
##----- The 'min.is.0' option : ------
##' dip(.) continuity and 'min.is.0' exploration:
dd <- function(x, debug=FALSE) {</pre>
   x_ <- x ; x_[1] <- 0.999999999 * x[1]</pre>
   rbind(dip(x , debug=debug),
         dip(x_, debug=debug),
         dip(x , min.is.0=TRUE, debug=debug),
         dip(x_, min.is.0=TRUE, debug=debug), deparse.level=2)
}
dd( rep(1, 8) ) # the 3rd one differs ==> min.is.0=TRUE is *dis*continuous
                # ditto
dd( 1:7 )
dd( 1:7, debug=TRUE)
## border-line case ..
dd( 1:2, debug=TRUE)
## Demonstrate that 'min.is.0 = TRUE' does not change the typical result:
B.sim <- 1000 # or larger
D5 <- {set.seed(1); replicate(B.sim, dip(runif(5)))}</pre>
D5. <- {set.seed(1); replicate(B.sim, dip(runif(5), min.is.0=TRUE))}</pre>
stopifnot(identical(D5, D5.), all.equal(min(D5), 1/(2*5)))
hist(D5, 64); rug(D5)
D8 <- {set.seed(7); replicate(B.sim, dip(runif(8)))}</pre>
D8. <- {set.seed(7); replicate(B.sim, dip(runif(8), min.is.0=TRUE))}</pre>
stopifnot(identical(D8, D8.))
```

dip.test

Hartigans' Dip Test for Unimodality

#### Description

Compute Hartigans' dip statistic  $D_n$ , and its p-value for the test for unimodality, by interpolating tabulated quantiles of  $\sqrt{n}D_n$ .

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#### dip.test

For  $X_i \sim F$ , *i.i.d.*, the null hypothesis is that F is a unimodal distribution. Consequently, the test alternative is non-unimodal, i.e., at least bimodal. Using the language of medical testing, you would call the test "Test for **Multi**modality".

#### Usage

```
dip.test(x, simulate.p.value = FALSE, B = 2000)
```

#### Arguments

х	numeric vector; sample to be tested for unimodality.
simulate.p.valu	Je
	a logical indicating whether to compute p-values by Monte Carlo simulation.
В	an integer specifying the number of replicates used in the Monte Carlo test.

#### Details

If simulate.p.value is FALSE, the p-value is computed via linear interpolation (of  $\sqrt{n}D_n$ ) in the qDiptab table. Otherwise the p-value is computed from a Monte Carlo simulation of a uniform distribution (runif(n)) with B replicates.

#### Value

A list with class "htest" containing the following components:

statistic	the dip statistic $D_n$ , i.e., dip(x).
p.value	the p-value for the test, see details.
method	character string describing the test, and whether Monte Carlo simulation was used.
data.name	a character string giving the name(s) of the data.

#### Note

see also the package vignette, which describes the procedure in more details.

#### Author(s)

Martin Maechler

#### References

see those in dip.

#### See Also

For goodness-of-fit testing, notably of continuous distributions, ks.test.

#### Examples

```
## a first non-trivial case
(d.t <- dip.test(c(0,0, 1,1))) # "perfect bi-modal for n=4" --> p-value = 0
stopifnot(d.t$p.value == 0)
data(statfaculty)
plot(density(statfaculty)); rug(statfaculty)
(d.t <- dip.test(statfaculty))
x <- c(rnorm(50), rnorm(50) + 3)
plot(density(x)); rug(x)
## border-line bi-modal ... BUT (most of the times) not significantly:
dip.test(x)
dip.test(x)
dip.test(x, simulate=TRUE, B=5000)
## really large n -- get a message
dip.test(runif(4e5))
```

```
exHartigan
```

Hartigan's Artificial n-modal Example Data Set

#### Description

63 (integer) numbers; unimodal or bimodal, that's the question. This is now *deprecated*. Please use statfaculty instead!

#### Examples

```
data(exHartigan)
plot(dH <- density(exHartigan))
rug(exHartigan)# should jitter</pre>
```

plot.dip

Plot a dip() Result, i.e., Class "dip" Object

#### Description

Plot method for "dip" objects, i.e., the result of dip(., full.result=TRUE) or similar.

Note: We may decide to enhance the plot in the future, possibly not entirely back-compatibly.

#### Usage

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#### qDiptab

#### Arguments

x	an R object of class "dip", i.e., typically the result of dip(., full.result= FF) where FF is TRUE or a string such as "all".
do.points	logical indicating if the ECDF plot should include points; passed to plot.ecdf.
colG, colL, colM	Ч
	the colors to be used in the graphics for the Greatest convex minorant, the Least concave majorant, and the Modal interval, respectively.
col.points, col	hor
	the color of points or horizontal lines, respectively, simply passed to plot.ecdf.
doModal	logical indicating if the modal interval $[x_L, x_U]$ should be shown.
doLegend	logical indicating if a legend should be shown.
	further optional arguments, passed to plot.ecdf.

#### Author(s)

Martin Maechler

#### See Also

dip, also for examples; plot.ecdf.

qDiptab

Table of Quantiles from a Large Simulation for Hartigan's Dip Test

#### Description

Whereas Hartigan(1985) published a table of empirical percentage points of the dip statistic (see dip) based on N=9999 samples of size n from U[0, 1], our table of empirical quantiles is currently based on N=1'000'001 samples for each n.

#### Format

A numeric matrix where each row corresponds to sample size n, and each column to a probability (percentage) in [0, 1]. The dimnames are named n and Pr and coercable to these values, see the examples. attr(qDiptab, "N\_1") is N-1, such that with k <- as.numeric(dimnames(qDiptab)\$Pr) \* attr(qDiptab, "N\_1"), e.g., qDiptab[n == 15,] contains exactly the order statistics  $D_{[k]}$  (from the N + 1 simulated values of dip(U), where U <- runif(15).

#### Note

Taking N=1'000'001 ensures that all the quantile(X, p) used here are exactly order statistics sort(X)[k].

#### Author(s)

Martin Maechler <maechler@stat.math.ethz.ch>, in its earliest form in August 1994.

#### See Also

dip, also for the references; dip.test() which performs the hypothesis test, using qDtiptab (and its null hypothesis of a uniform distribution).

#### Examples

```
data(qDiptab)
str(qDiptab)
## the sample sizes `n' :
dnqd <- dimnames(qDiptab)
(nn <- as.integer(dnqd $n))
## the probabilities:
P.p <- as.numeric(print(dnqd $ Pr))
## This is as "Table 1" in Hartigan & Hartigan (1985) -- but more accurate
ps <- c(1,5,10,50,90,95,99, 99.5, 99.9)/100
tab1 <- qDiptab[nn <= 200, as.character(ps)]
round(tab1, 4)</pre>
```

statfaculty

Faculty Quality in Statistics Departments

#### Description

Faculty quality in statistics departments was assessed as part of a larger study reported by Scully(1982). Accidentally, this is also provided as the exHartigan ("example of Hartigans") data set.

#### Usage

```
data(statfaculty)
```

#### Format

A numeric vector of 63 (integer) numbers, sorted increasingly, as reported by the reference.

#### Source

M. G. Scully (1982) Evaluation of 596 programs in mathematics and physical sciences; *Chronicle Higher Educ.* **25** 5, 8–10.

#### References

J. A. Hartigan and P. M. Hartigan (1985) The Dip Test of Unimodality; Annals of Statistics 13, 70-84.

#### statfaculty

### Examples

```
data(statfaculty)
plot(dH <- density(statfaculty))
rug(jitter(statfaculty))</pre>
```

data(exHartigan)
stopifnot(identical(exHartigan,statfaculty))

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