

Package ‘LATERmodel’

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Title Linear Approach to Threshold with Ergodic Rate for Reaction Times

Version 0.2.0

Description Implements the Linear Approach to Threshold with Ergodic Rate (LATER) model, which predicts distributions of reaction times and summarises them with as little as two free parameters. Allows for easy visualisation and comparison of datasets, along with fitting of datasets using the LATER model.

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Imports dplyr, ggplot2, rlang, stats, tibble, parallel, moments

Depends R (>= 4.1)

LazyData true

Suggests lintr, styler, testthat (>= 3.0.0), vdiff, printr, withr

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URL <https://github.com/unimelbmdap/LATERmodel>,
<https://unimelbmdap.github.io/LATERmodel/>

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carpenter_williams_1995

Digitised data corresponding to Figure 2 of Carpenter and Williams (1995)

Description

Digitised data corresponding to Figure 2 of Carpenter and Williams (1995)

Usage

carpenter_williams_1995

Format

carpenter_williams_1995:

A dataframe of 20014 reaction times for participant a and 22518 reaction times for participant b

participant Participant "name", either "a" or "b"

condition Prior percentage probability of the target being in the location of the eye movement (p05, p10, p25, p50, p75, p90, or p95)

time Saccadic latency in ms

Source

Carpenter, R. H., & Williams, M. L. L. (1995). Neural computation of log likelihood in control of saccadic eye movements. *Nature*, 377(6544), 59-62.

compare_fits	<i>Compares the goodness-of-fit of a set of fit outcomes.</i>
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Description

Compares the goodness-of-fit of a set of fit outcomes.

Usage

```
compare_fits(fits)
```

Arguments

fits A list where each item has a name that identifies the fit and a value given by the output of `LATERmodel::fit_data`.

Details

The 'evidence ratio' is calculated as per Motulsky & Christopolous (2004), p. 146.

Value

A list of fit comparison results, ordered such that the fit with the lowest AIC value is in the first row.

- `aic` contains the fit AIC values.
- `preferred_rel_fit_delta_aic` is the AIC value for the fit relative to the AIC of the fit with the lowest AIC (preferred AIC - current AIC).
- `preferred_rel_fit_evidence_ratio` is the evidence ratio for the fit with the lowest AIC relative to the current fit.
- `preferred` is a boolean that indicates whether the fit has the lowest AIC value among the fits (is 'preferred').

Examples

```
data <- rbind(
  data.frame(name = "test", time = 1000/rnorm(100, 3, 1)),
  data.frame(name = "test_2", time = 1000/rnorm(100, 1, 1))
) |> dplyr::filter(time > 0)
data <- prepare_data(data)
fit_a <- fit_data(data = data, share_a = TRUE)
fit_b <- fit_data(data = data, share_sigma = TRUE)
comparison <- compare_fits(fits = list(a = fit_a, b = fit_b))
```

fit_data

Fit a LATER model to a single dataset or a pair of datasets.

Description

Fit a LATER model to a single dataset or a pair of datasets.

Usage

```
fit_data(
  data,
  share_a = FALSE,
  share_sigma = FALSE,
  share_sigma_e = FALSE,
  with_early_component = FALSE,
  intercept_form = FALSE,
  use_minmax = FALSE,
  fit_criterion = "likelihood",
  jitter_settings = list(n = 7, prop = 0.5, seed = NA, processes = 2)
)
```

Arguments

data	A data frame with columns name and promptness.
share_a, share_sigma, share_sigma_e	If FALSE (the default), each dataset has its own parameter. If TRUE, the datasets share the relevant parameter.
with_early_component	If TRUE, the model contains a second 'early' component that is absent when FALSE (the default).
intercept_form	If FALSE (the default), the a parameter describes the mu parameter in the model; if TRUE, the a parameter describes the k parameter in the model (the intercept).
use_minmax	If FALSE (the default), the optimiser targets the sum of the goodness-of-fit values across datasets; if TRUE, it instead targets the maximum of the goodness-of-fit values across datasets.
fit_criterion	String indicating the criterion used to optimise the fit by seeking its minimum. <ul style="list-style-type: none"> ks: Kolmogorov-Smirnov statistic. likelihood: Negative log-likelihood.
jitter_settings	Settings for running the fitting multiple times with randomly-generated offsets ('jitter') applied to the starting estimates. <ul style="list-style-type: none"> n: How many jitter iterations to run (default of 7); the total number of fits is n + 1 (because the un-jittered start points are also fit). prop: The maximum jitter offset, as a proportion of the start value (default of 0.5).

- `seed`: Seed for the random jitter generator (default is unseeded).
- `processes`: Maximum number of CPU processes that can be used (default is 2).

Value

A list of fitting arguments and outcomes.

- `fitted_params` is a named list of fitted parameter values.
- `named_fit_params` is a data frame with rows given by the dataset names and columns given by the parameter names.
- `loglike` is the overall log-likelihood of the fit.
- `aic` is the "Akaike's 'An Information Criterion'" value for the model.
- `optim_result` is the raw output from `stats::optim` for the best fit.
- `jitter_optim_results` contains the raw output from each call to `stats::optim` for the different start points.

Examples

```
data <- data.frame(name = "test", promptness = rnorm(100, 3, 1))
data_other <- data.frame(name = "test_2", promptness = rnorm(100, 1, 1))
fit_shared_sigma <- fit_data(
  data = rbind(data, data_other), share_sigma = TRUE
)
```

`individual_later_fit` *Fit individual LATER model to each dataset in a dataframe of datasets*

Description

Fit individual LATER model to each dataset in a dataframe of datasets

Usage

```
individual_later_fit(
  df,
  with_early_component = FALSE,
  fit_criterion = "likelihood",
  jitter_settings = list(n = 7, prop = 0.5, seed = NA, processes = 2)
)
```

Arguments

- `df` A dataframe with columns: time, name, promptness, and e_cdf
- `with_early_component` If TRUE, the model contains a second 'early' component that is absent when FALSE (the default).
- `fit_criterion` String indicating the criterion used to optimise the fit by seeking its minimum.
- `ks`: Kolmogorov-Smirnov statistic.
 - `neg_logLike`: Negative log-likelihood.
- `jitter_settings` Settings for running the fitting multiple times with randomly-generated offsets ('jitter') applied to the starting estimates.
- `n`: How many jitter iterations to run (default of 7).
 - `prop`: The maximum jitter offset, as a proportion of the start value (default of 0.5).
 - `seed`: Seed for the random jitter generator (default is unseeded).
 - `processes`: Maximum number of CPU processes that can be used (default is 2).

Value

A dataframe with one row for each named dataset in `df` and columns equal to the LATER model parameters returned by `fit_data$named_fit_params`

Examples

```
data <- rbind(
  data.frame(name = "test", promptness = rnorm(100, 3, 1)),
  data.frame(name = "test_2", promptness = rnorm(100, 1, 1))
)
fit_params <- individual_later_fit(data)
```

<code>ks_compare</code>	<i>Apply two-sample KS test to all pairs of datasets contained within a dataframe</i>
-------------------------	---

Description

Apply two-sample KS test to all pairs of datasets contained within a dataframe

Usage

```
ks_compare(df, correct_multiple_comparisons = TRUE)
```

Arguments

`df` A dataframe of datasets with columns: name and time, one unique name per dataset

`correct_multiple_comparisons` If TRUE, an adjustment will be made to the p-values based on Holm, 1979, A simple sequentially rejective multiple test procedure

Value

A dataframe with columns name1, name2, D, and p_value

Examples

```
data <- prepare_data(dplyr::filter(
  carpenter_williams_1995,
  participant == "b"
))
ks_compare(data)
```

<code>ks_heatmap</code>	<i>Create a heatmap to visualise if there is not enough evidence to reject the null hypothesis that two datasets come from the same underlying distribution</i>
-------------------------	---

Description

Create a heatmap to visualise if there is not enough evidence to reject the null hypothesis that two datasets come from the same underlying distribution

Usage

```
ks_heatmap(ks_results)
```

Arguments

`ks_results` A dataframe with columns name1, name2, D, and p-value, obtained using the function `ks_compare`

Value

A heatmap plot with all paired comparisons

Examples

```
data <- prepare_data(dplyr::filter(
  carpenter_williams_1995,
  participant == "b"
))
ks_results <- ks_compare(data)
ks_heatmap(ks_results)
```

model_cdf	<i>Evaluate the cumulative distribution function under the model.</i>
-----------	---

Description

Evaluate the cumulative distribution function under the model.

Usage

```
model_cdf(q, later_mu, later_sd, early_sd = NULL)
```

Arguments

q	Vector of quantiles
later_mu	Vector of the mean of the later component.
later_sd	Vector of the standard deviation of the later component.
early_sd	Vector of the standard deviation of the early component, or NULL if there is no early component (the default).

Value

Vector of cumulative distribution values

Examples

```
model_cdf(q = 1, later_mu = 1, later_sd = 1)
model_cdf(q = 1, later_mu = 1, later_sd = 1, early_sd = 3)
```

model_pdf	<i>Evaluate the probability density function under the model.</i>
-----------	---

Description

Evaluate the probability density function under the model.

Usage

```
model_pdf(x, later_mu, later_sd, early_sd = NULL, log = FALSE)
```

Arguments

x	Vector of quantiles
later_mu	Vector of the mean of the later component.
later_sd	Vector of the standard deviation of the later component.
early_sd	Vector of the standard deviation of the early component, or NULL if there is no early component (the default).
log	If TRUE, probabilities are given as $\log(p)$.

Value

Vector of probabilities

Examples

```
model_pdf(x = 1, later_mu = 1, later_sd = 1)
model_pdf(x = 1, later_mu = 1, later_sd = 1, early_sd = 3)
```

prepare_data	<i>Prepares data for reciprobit plot</i>
--------------	--

Description

Prepares data for reciprobit plot

Usage

```
prepare_data(raw_data, time_unit = "ms", name_separator = "_")
```

Arguments

raw_data	Vector of reaction times for a single participant, or a dataframe containing a column called time with the reaction times and optional other columns: <ul style="list-style-type: none"> • a column called name with a unique label for each dataset • a column called participant with a unique id per participant and another called condition with a unique label for each condition. In this case the name for each dataset will be constructed as participant+name_separator+condition. • a column called color that contains one hexadecimal color code for each dataset. In this case the name for each dataset will be set to be the name of the color.
time_unit	Units of the reaction times in rt_vector, must be one of "ms", "ds", or "s".
name_separator	If the raw_data dataframe does not contain a name column, but does have participant and condition columns, the name for each dataset will be constructed as participant+name_separator+condition.

Value

A dataframe with columns: time, color, name, promptness, and e_cdf.

Examples

```
df <- prepare_data(carpenter_williams_1995)
```

promptness_ecdf	<i>Compute the empirical cumulative distribution function for promptness</i>
-----------------	--

Description

Compute the empirical cumulative distribution function for promptness

Usage

```
promptness_ecdf(promptness, adjust_for_times = TRUE, eval_unique = FALSE)
```

Arguments

promptness	A vector of promptness values (1 / times)
adjust_for_times	If TRUE (the default), the returned y value is such that $1 - y = P(1/\text{promptness} \leq 1/x)$. If FALSE, the returned y value is $P(\text{promptness} \leq x)$.
eval_unique	If FALSE (the default), the ECDF is evaluated at all values in promptness. If TRUE, the ECDF is evaluated at the unique values in promptness.

Value

A data frame with attributes:

- x is the values at which the ECDF was evaluated.
- y is the evaluated value of the ECDF.

Examples

```
p <- promptness_ecdf(promptness = rnorm(100, 3, 1))
```

reciprobit_plot	<i>Plot reaction times and LATER model fit in reciprobit axes</i>
-----------------	---

Description

Plot reaction times and LATER model fit in reciprobit axes

Usage

```

reciprobit_plot(
  plot_data,
  fit_params = NULL,
  time_breaks = c(0.1, 0.2, 0.3, 0.5, 1),
  probit_breaks = c(0.1, 1, 5, 10, 20, 50, 80, 90, 95, 99, 99.9),
  z_breaks = c(-2, -1, 0, 1, 2),
  xrange = NULL,
  yrange = NULL
)

```

Arguments

<code>plot_data</code>	A dataframe with columns: time, name, promptness, and e_cdf. Optionally, there may be a color column, which contains hex values, one unique hex value per named dataset
<code>fit_params</code>	A dataframe with one row for each named dataset and columns equal to the LATER model parameters returned by <code>fit_data\$named_fit_params</code>
<code>time_breaks</code>	Desired tick marks on the x axis, expressed in promptness (1/s)
<code>probit_breaks</code>	Desired tick marks on the y axis in probit space
<code>z_breaks</code>	Desired tick marks on secondary y axis, in z values
<code>xrange</code>	Desired range for the x axis, in promptness (1/s)
<code>yrange</code>	Desired range for the y axis, in cumulative probability space

Value

A reciprobbit plot with the cumulative probability distribution of the reaction times

Examples

```

data <- rbind(
  data.frame(name = "test", time = 1000/rnorm(100, 3, 1)),
  data.frame(name = "test_2", time = 1000/rnorm(100, 4, 1))
) |> dplyr::filter(time > 0)
data <- prepare_data(data)
fit_params <- individual_later_fit(data)
reciprobit_plot(data, fit_params)

```

reddi_asrress_carpenter_2003

Digitised data corresponding to Figure 2 of Reddi, Asrress, and Carpenter, 2003.

Description

Digitised data corresponding to Figure 2 of Reddi, Asrress, and Carpenter, 2003.

Usage

```
reddi_asrress_carpenter_2003
```

Format

```
reddi_asrress_carpenter_2003:
```

A dataframe of 1600 reaction times for participant J

participant Participant "name", equal to "J"

condition Different degrees of coherence of the kinematograms shown as stimuli, (64%, 32%, 16%, 8%: S, low-urgency–slow and accurate–conditions)

time Saccadic latency in ms

Source

Reddi, B. A., Asrress, K. N., & Carpenter, R. H. (2003). Accuracy, information, and response time in a saccadic decision task. *Journal of Neurophysiology*, 90(5), 3538-3546.

```
simulate_dataset
```

Simulate a dataset given model parameters.

Description

Generates samples from a set of provided LATER model parameters, with the option to iteratively replace invalid samples (reaction times ≤ 0).

Usage

```
simulate_dataset(  
  n,  
  later_mu,  
  later_sd,  
  early_sd = NULL,  
  seed = NA,  
  allow_negative_times = FALSE  
)
```

Arguments

n	Number of samples (trials)
later_mu	Mean of the later component.
later_sd	Standard deviation of the later component.

<code>early_sd</code>	Standard deviation of the early component, or NULL if there is no early component (the default).
<code>seed</code>	Seed for the random number generator
<code>allow_negative_times</code>	If FALSE (the default), any random samples that have negative response times are iteratively replaced such that all returned samples are positive. If TRUE, no such replacement is performed.

Value

Vector of response times (in seconds)

Examples

```
simulate_dataset(n = 100, later_mu = 5, later_sd = 1)
simulate_dataset(n = 100, later_mu = 5, later_sd = 1, early_sd = 5)
```

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