

# There Is No Largest Prime Number

With an introduction to a new proof technique

Euklid of Alexandria

Department of Mathematics  
University of Alexandria

27th International Symposium on Prime Numbers,  
–280

## Results

Proof of the Main Theorem

# There Is No Largest Prime Number

The proof uses *reductio ad absurdum*.

There Is No  
Largest Prime  
Number

Euklid

Results

Proof of the Main Theorem

## Theorem

*There is no largest prime number.*

## Proof.

1. Suppose  $p$  were the largest prime number.
2. Let  $q$  be the product of the first  $p$  numbers.
3. Then  $q + 1$  is not divisible by any of them.
4. Thus  $q + 1$  is also prime and greater than  $p$ . □